

GWA in presence of population stratification

Yurii Aulchenko
Erasmus MC Rotterdam
26.08.2009

ESP29, 26.08.2009

Yurii Aulchenko

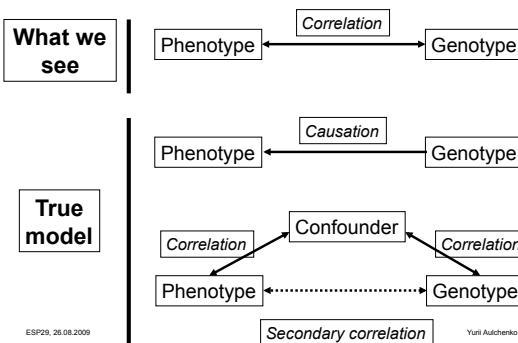
Outline

- Confounding and stratification in GWA studies
- Genomic Control and Structured Association
- PCA correction (EIGENSTRAT)
- Quality Control (QC) of genetic data

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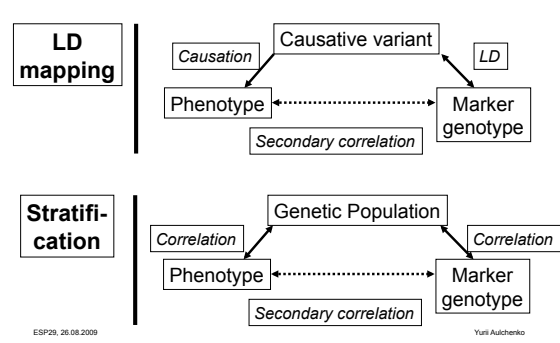
Reasons for genetic association



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Confounding in genetic studies



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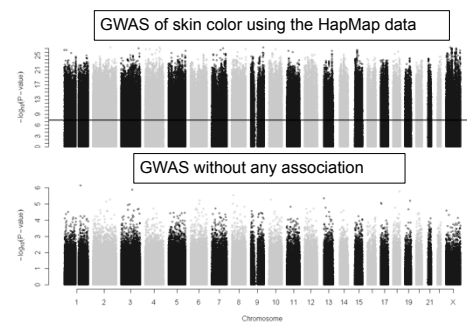
Stratification

- Some factor is a confounder for genotypes and disease prevalence
 - Dark skin is more prevalent in people Africans than in Europeans. The genotypic frequencies are also different between two populations.
 - A study of skin color, which would mix Africans and Europeans is likely to generate multiple false positives
- Other causes of genetic stratification are “cryptic” relations or systematic pedigree structure presented in a sample

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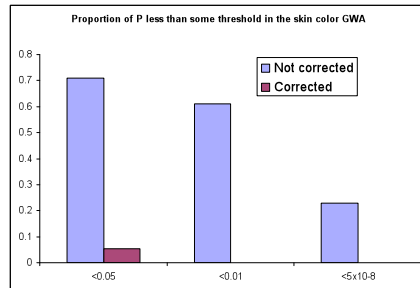
Skin color scan



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Consequences of stratification



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Outline

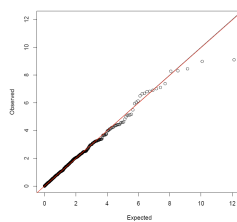
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Distribution of the test statistics under the null hypothesis

- 200 random SNPs
- In Linkage Equilibrium
- Not related to the disease
- No stratification
- The distribution of the test statistics for association is χ^2_1

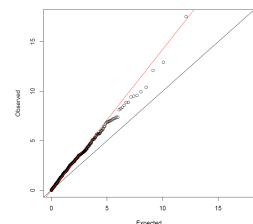


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Idea of the genomic control

- There is stratification
- **Assumption: stratification acts in the same manner across all loci**
- This leads to uniform inflation of the test statistics
- The distribution of the test statistics is $\lambda \cdot \chi^2_1$ ($\lambda \geq 1$)



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Genomic control

- Consider a test distributed as χ^2_1 under the null (e.g. trend test)
- Select N (>200) independent SNPs and compute the vector of test statistics $\{T^2_1, T^2_2, T^2_3, \dots, T^2_{N-1}, T^2_N\}$
- Estimate λ as
 - $\text{Median}\{T^2_1, T^2_2, T^2_3, \dots, T^2_{N-1}, T^2_N\} / 0.456$
 - Slope of regression of observed onto expected
- The GC-corrected test statistics
 - $T^2 / \lambda \sim \chi^2_1$
- In practice, all (or large proportion of) GW test are used to estimate λ .

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λ is dependent on sample size

- λ is related to non-centrality parameter, thus it grows with sample size. Therefore λ should be estimated per certain sample size. This is especially important if
 - SNP call rate is very different between SNPs
 - When reporting the results
- For QT analysis, $\lambda_n = 1 + (\lambda_{n_{\text{ref}}} - 1) n / n_{\text{ref}}$ where n_{ref} is the reference sample size
- For case/control design

$$\lambda_{n_j, m_j} = 1 + (\lambda_{n_{\text{ref}}, m_{\text{ref}}} - 1) \left(\frac{1}{n_j} + \frac{1}{m_j} \right) / \left(\frac{1}{n_{\text{ref}}} + \frac{1}{m_{\text{ref}}} \right)$$

where n & m refer to size of samples of cases and controls

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When GC does not work (well)?

When stratification is large (say, $\lambda_{1000} > 1.1$) other, more powerful methods are to be used

GC assumes that stratification acts in the same manner across all loci

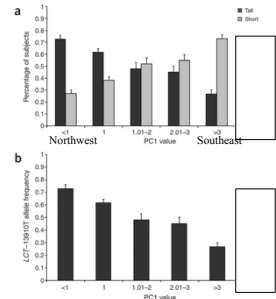
- This is not true for loci differentiated between population e.g. because of selection
- Such loci will still be falsely detected after GC correction

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Example: association of stature to LCT

- SNP in the lactase (LCT) gene was strongly associated with height ($P < 10^{-6}$)
- GC λ was 1.0
- The LCT SNP is selected and differentiated between European populations
- Little evidence left after applying structured association



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•Campbell et al, Nat Genet 2005

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Structured association (SA)

- Identify genetic populations (strata)
- Mantel-Haenszel test for structured association
- Basically, components of the score test (association score and its' variance) are computed in each strata separately. These could be added up and give single test
- Apply GC to correct for residual inflation ($1 < \lambda < 1.1$)
- Problems with SA
 - Strata not always known or easy to identify
 - Is not powerful when there is a strong case/control mismatch

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Idea of Multidimensional Scaling

- Study of N subjects
- $N \times N$ matrix of pair-wise distances (0 = the same subject, 1 = very different)
- Multi-Dimensional (MD) scaling takes this matrix
 - Returns coordinates for N points in a MD-space
 - The vectors are called "Principal Axes of Variation" (or Principal Components)
 - The distance between the points in this MD-space are as close as possible to the distances observed in the original $N \times N$ matrix
- Classical MDS is also known as Principal Components Analysis

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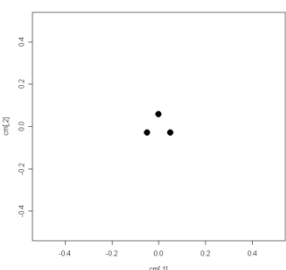
Example CMDS

- Distance matrix

	ID1	ID2	ID3
ID1	0	0.1	0.1
ID2	0.1	0	0.1
ID3	0.1	0.1	0

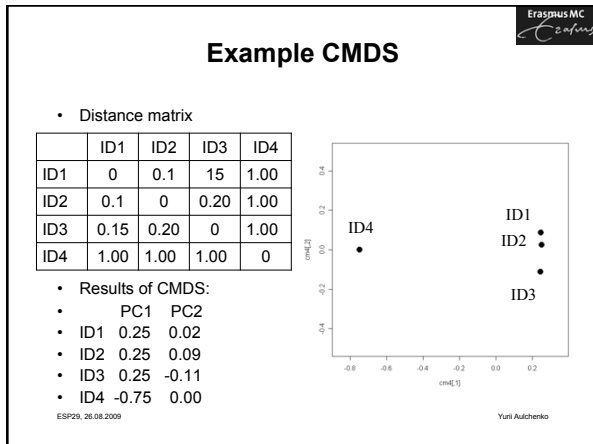
- Results of CMDS:

- PC1 PC2
- ID1 0.00 0.29
- ID2 -0.25 -0.14
- ID3 0.25 -0.14



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Relationship matrix from genomic data

2 x Kinship between people i and j is the expected proportion of genome shared identical by descent

Distance matrix: 0.5 - kinship

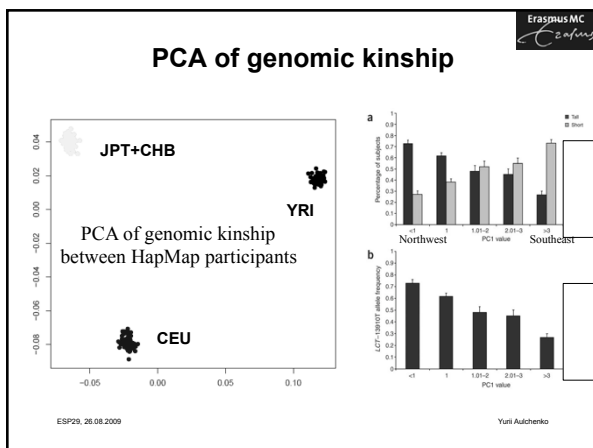
Genomic estimate of kinship between i and j is computed with

$$f_{ij} = \frac{1}{n} \sum_{k=1}^n \frac{(g_{ik} - p_k)(g_{jk} - p_k)}{p_k(1 - p_k)}$$

g_{ik} is the genotype (0, 0.5, 1) of the i -th person at k -th SNP
 p_k is the frequency of "1" allele

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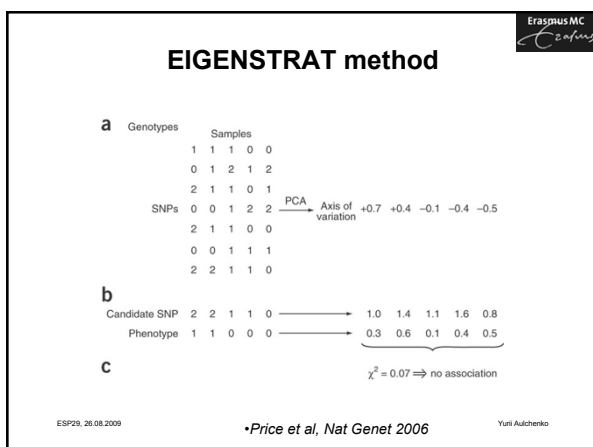
Idea of EIGENSTRAT method

- Quantify genetic origin of study participants with a number (3 to 10) principal axes of variation returned from CMDS analysis of genomic kinship matrix
- In analysis of association, adjust both phenotypes and genotypes for these principal axes of variation
- Apply GC to correct for residual inflation ($1 < \lambda < 1.1$)
- EIGENSTRAT can also (at least partly) correct for differences between genotyping cohorts

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•Price et al, Nat Genet 2006



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Using genomic kinship PC as covariates

- One can use PCs for adjustment using liner model

$$\text{Trait} \sim m + \text{SNP} + \text{PC}_1 + \text{PC}_2 + \dots$$

- A problem of using PCs: what PCs to include? How many?

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Summary

- If homogeneous group is studied
 - Detect (hopefully few) genetic outliers
 - Remove them from analysis
 - Apply GC to correct for residual stratification
 - Verify findings with EIGENSTRAT
- If multiple strata are expected by design
 - Identify genetic strata
 - Cross-validate with external information
 - If case/control matching is good, apply SA
 - Else, apply EIGENSTRAT analysis
- If strata are not known/difficult to identify
 - Apply EIGENSTRAT / PC adjustment
 - Apply methods using genomic kinship matrix as a whole