

# IBD computations in large pedigrees

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# IBD computation in large pedigrees

Is part of a problem of computation of the likelihood function of a pedigree

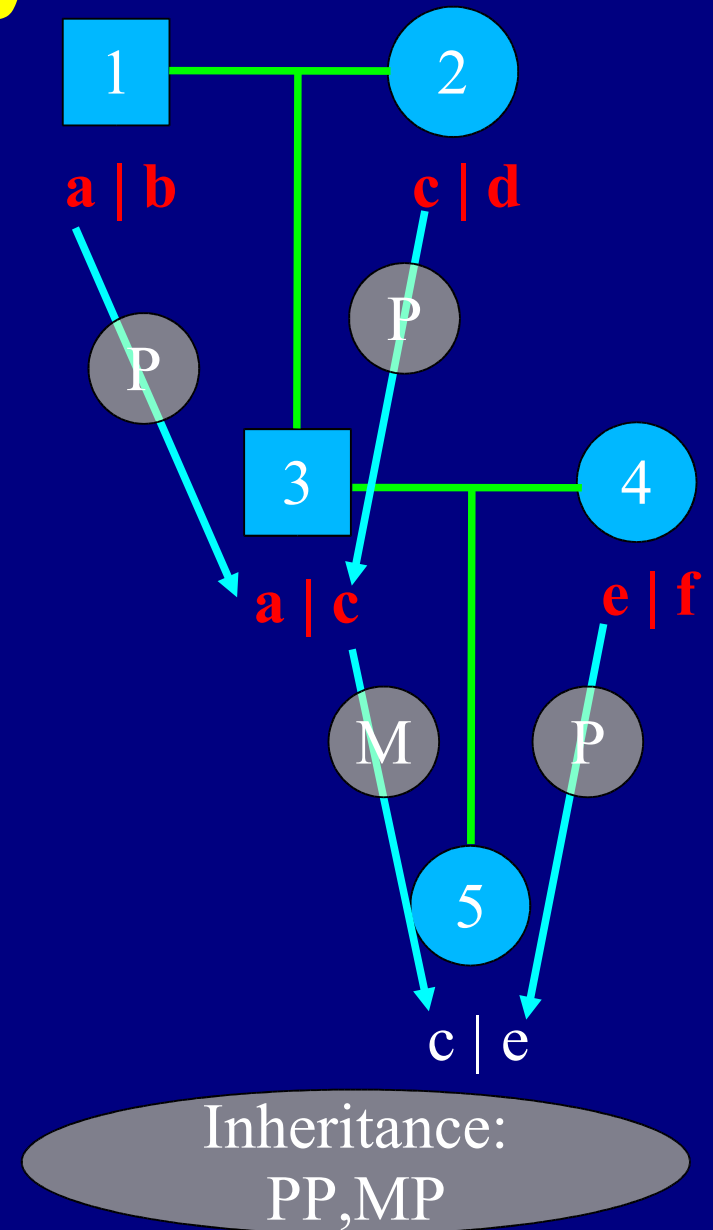
# Computation of the likelihood

- $X$  – matrix of phenotypes (trait, marker data) of pedigree members
- $G$  – matrix of underlying genotypes of pedigree members
- Likelihood:

$$\sum_{\text{all } G} P(X|G)P(G)$$

# Complexity

- How much is “all G”?
  - Number of genotypes possible for a founder
    - by
  - number of inheritance patterns



# Complexity

- How much is “all G”?
  - Number of genotypes possible for a founder:
    - One trait locus, 1 marker with 10 alleles:
      - $2 \times 2 \times 10 \times 10 = 400$  combinations
    - One trait locus, 5 markers with 10 alleles:
      - $4 \times 10^5 = 40,000,000,000$  combinations
  - Number of inheritance patterns
    - 5 non-founders =  $2^{2 \times 5} = 1024$
    - 15 non founders =  $2^{2 \times 15} = 1,073,741,824$

# Computation time

- Sibship of 5:
  - 1 marker  $\Rightarrow$  2 sec.
  - 2 markers  $\Rightarrow$  4.5 hours
  - 3 markers  $\Rightarrow$  5 years

## Trait locus + 2 markers

- 6 sibs  $\Rightarrow$  18 hours
- 8 sibs  $\Rightarrow$  12 days
- 10 sibs  $\Rightarrow$   $\frac{1}{2}$  year

# Peeling

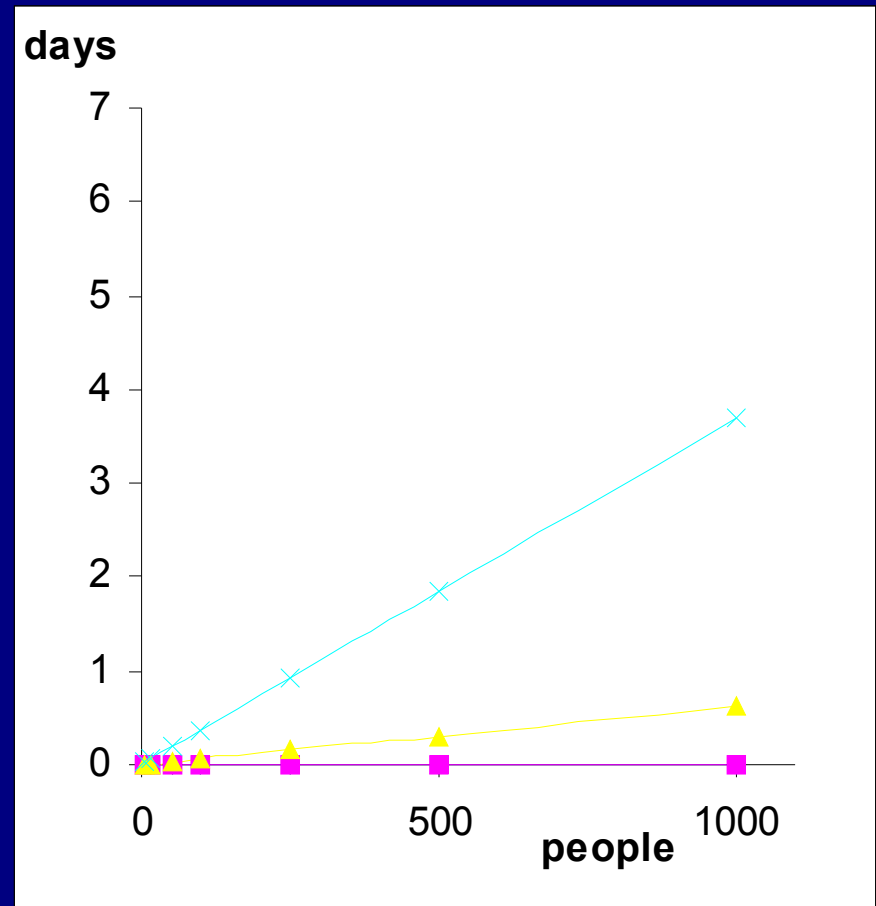
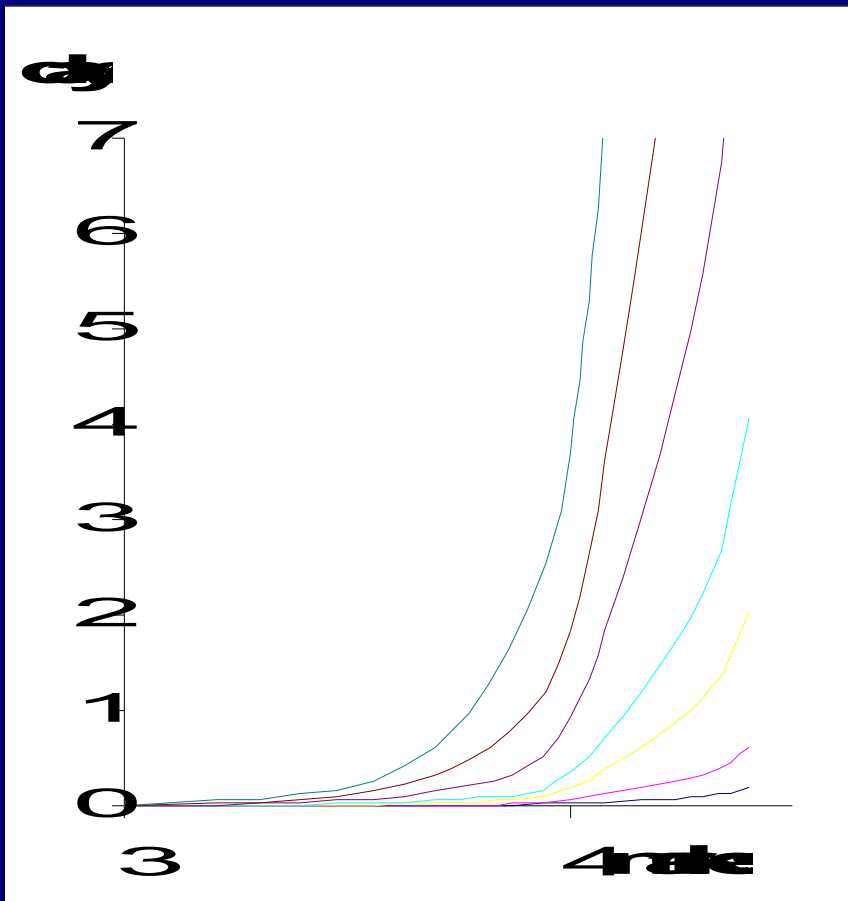
- A computational technique which reduces the complexity of computations by sequential computations over conditionally independent events

# Elston-Stewart peeling

- For parts of pedigree, compute probability conditional on all possible genotypes of members who connect this part to the rest
- Computation time
  - ~  $\text{No\_people} * (\text{no\_possible\_genotypes}) * (\text{no\_loop-breakers})$
  - Grows
    - linear with no. people
    - exponential with no. markers



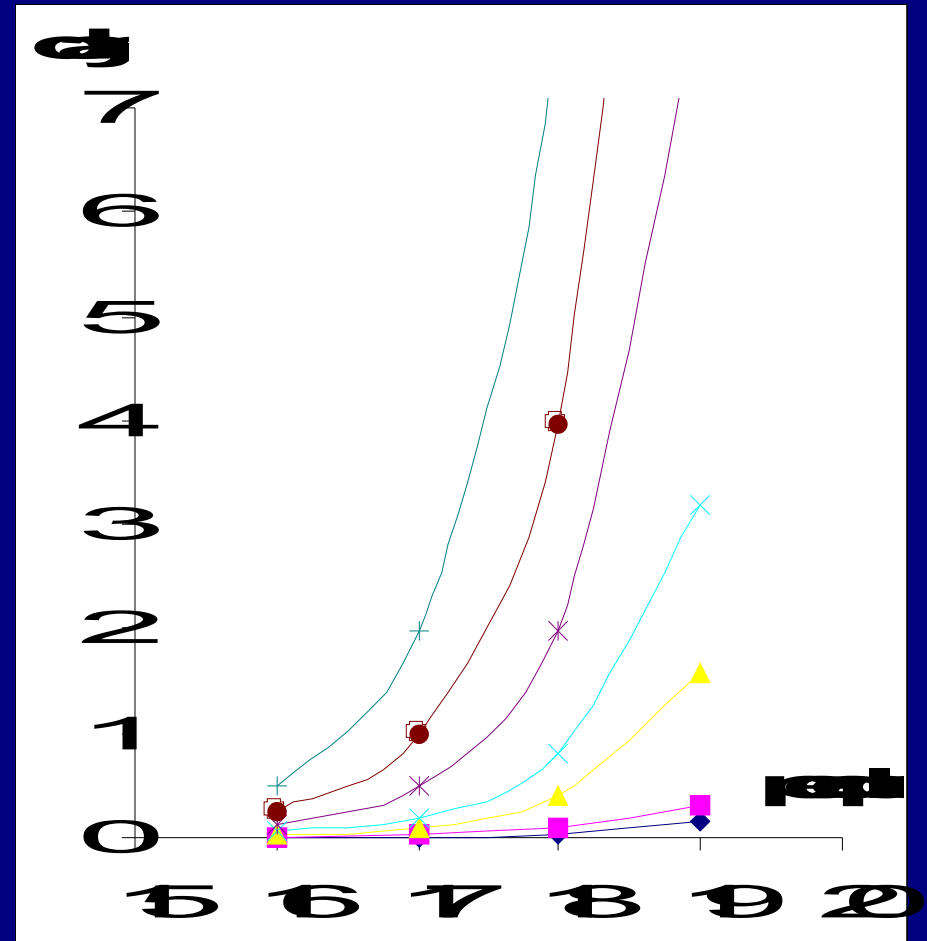
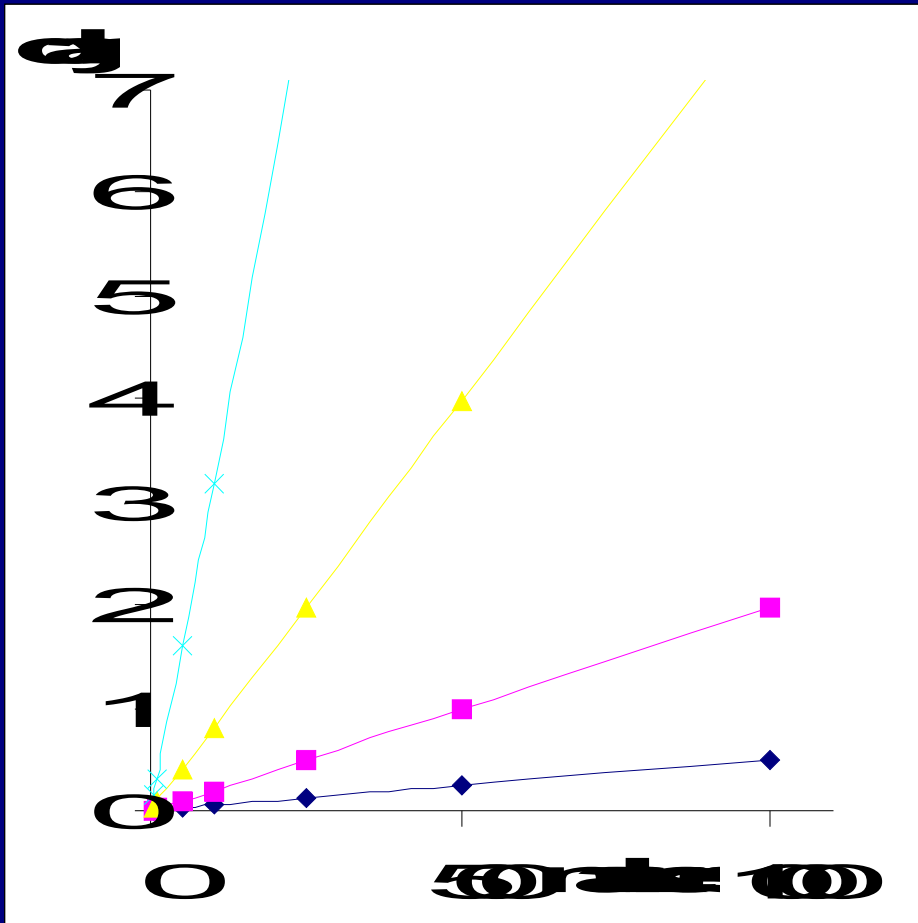
# Computation time for ES-algorithm



# Lander-Green peeling

- For particular marker (phenotype), compute probability for all pedigree members conditional on flanking genotypes
  - Computation time
    - ~ No\_loci \* (no\_possible\_inheritance\_patterns)
- Grows**
- Exponential with no. people
  - Linear with no. markers

# Computation time for LG-algorithm



# Limitations of exact methods

- E-S algorithm:
  - 3-4 markers and 2-3 loops is absolute maximum
- LG algorithm:
  - BIT-SIZE ~ 20-28
    - BIT-SIZE =  $(2 * \text{no\_non-founders} - \text{no\_founders})$

# Markov Chain Monte-Carlo

- A technique to compute approximate probabilities
- Can run well for few hundreds of people and few dozens of loops (takes weeks to finish)
- Very efficient on pedigrees ~50-70 people
- Results depend on the choice of random numbers

# Programs for IBD computation

- Exact IBD using Elston-Stewart algorithm  
MERLIN, ALLEGRO, GENEHUNTER
- Exact single-marker IBD for zero-loop pedigrees  
SOLAR
- MCMC approximation  
SIMWALK2: great results, but very slow  
LOKI: can be faster, but user has to control convergence