

Genetic structure advanced practical

Yurii Aulchenko

February 18, 2013

Contents

1	Loading the libraries and data	1
2	GWAS with genomic control	2
3	Analyses accounting for population structure	2
4	Appendix A: Answers to exercises	3
5	Appendix B: Generation of the data set	9

1 Loading the libraries and data

Start R, load library GenABEL

```
library(GenABEL)
```

```
Loading required package: MASS  
GenABEL v. 1.7-4 (February 03, 2013) loaded
```

```
Installed GenABEL version (1.7-4) is not the same as stable  
version available from CRAN (1.7-3). Unless used intentionally,  
consider updating to the latest CRAN version. For that, use  
'install.packages("GenABEL")', or ask your system administrator  
to update the package.
```

Load the data set

```
load("data/hm.RData")
ls()
class(df)

[1] "df" "old"
[1] "gwaa.data"
attr("package")
[1] "GenABEL"
```

Characterize the data set:

Ex. 1 — How many people and SNPs are there in the data set?

Ex. 2 — Explore the phenotypic data. How many males/females are in the data? Look at the variable ‘pop’ – how many people from each population are present in the data set?

2 GWAS with genomic control

Use ‘qtscore’ function for GWAS of the phenotype ‘phe’.

Answer to the following questions:

Ex. 3 — What is the mean and standard deviation of ‘phe’?

Ex. 4 — Do you need to adjust for sex?

Ex. 5 — Perform GWAS of ‘phe’. If you ignore the fact that you did not account for the population structure and look at un-corrected P-values, do you get GW-significant results?

Ex. 6 — What is the genomic control λ for naive GWAS?

Ex. 7 — Are there any significant results left after GC correction?

Ex. 8 — **Advanced** Estimate λ using other estimators, such as mean, median, and trimmed mean. How much these vary?

Ex. 9 — **Challenge** Try to judge which λ estimator is better.

3 Analyses accounting for population structure

Perform analyses accounting for population structure in different ways.

Ex. 10 — Perform stratified analysis using the ‘qtscore’ function. What is the GC λ ? Do you get any GW-significant hits?

Ex. 11 — Estimate genomic kinship matrix (use ‘ibs’ function with default options to run IBS estimator; then do not forget to set the diagonal to 1 by ‘diag(myIbsMatrix)<-1’). Plot the first two PCs. Perform PC-adjusted GWAS using the ‘mlreg’ function for analysis. If time permits, 1) vary the number of PCA included and see what happens to λ 2) try analysis with ‘qtscore’. Explain the difference in results. with λ .

Ex. 12 — Use kinship matrix to estimate pseudo-heritability of ‘phe’ with ‘polygenic’, and then run mixed model with ‘mmscore’. What is the estimate of pseudo- h^2 ? What is the resulting λ ? Are results better/worse than these before? Why? If time permits, use correlation kinship for the same analysis.

Ex. 13 — What analysis method is the ‘best’ for this data set?

4 Appendix A: Answers to exercises

Answer (Ex. 1) — Run R commands

```
nids(df)
nsnps(df)
[1] 210
[1] 529279
```

Answer (Ex. 2) — Run R commands

```
table(phdata(df)$sex)
table(phdata(df)$pop)
```

```
0 1
105 105
```

```
CEU CHB JPT YRI
60 45 45 60
```

Answer (Ex. 3) — They are

```
mean(phdata(df)$phe)
```

```
sd(phdata(df)$phe)
[1] 166.0977
[1] 16.0122
```

Answer (Ex. 4) — Yes, you need to adjust for sex:

```
summary(lm(phe~sex,data=phdata(df)))
```

Call:

```
lm(formula = phe ~ sex, data = phdata(df))
```

Residuals:

	Min	1Q	Median	3Q	Max
	-37.547	-11.887	0.114	11.912	31.952

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	160.313	1.460	109.798	< 2e-16 ***
sex	11.569	2.065	5.603	6.63e-08 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 14.96 on 208 degrees of freedom

Multiple R-squared: 0.1311, Adjusted R-squared: 0.127

F-statistic: 31.39 on 1 and 208 DF, p-value: 6.633e-08

Answer (Ex. 5) — Yes, you get ~50000 GW-significant hits. Too many!

```
qts0 <- qtscore(phe~sex,data=df)
```

```
summary(qts0)
```

```
table(qts0[,"P1df"]<5e-8)
```

Summary for top 10 results, sorted by P1df

	Chromosome	Position	Strand	A1	A2	N	effB	se_effB	chi2.1df
rs7168440	15	3053736555	+	T	C	210	-12.85670	1.155925	123.7086
rs7166206	15	3053755920	+	G	A	205	-12.80976	1.162289	121.4657
rs7183892	15	3053654692	+	T	C	210	-12.64348	1.147217	121.4625
rs6494411	15	3053611621	+	T	C	208	-12.47627	1.132840	121.2922
rs289818	15	3053571597	+	A	G	209	-12.60420	1.144676	121.2455
rs289816	15	3053570721	-	T	C	210	-12.52065	1.137800	121.0938
rs4411464	15	3053771183	+	T	C	210	-12.61157	1.152967	119.6476

rs4721415	7	1543802799	+	A	G	209	13.03773	1.198578	118.3236
rs7178111	15	3053851271	+	T	C	209	-12.37196	1.163472	113.0746
rs7178104	15	3053881343	+	T	C	209	-12.45988	1.175327	112.3854
	P1df	effAB		effBB	chi2.2df		P2df		Pc1df
rs7168440	9.757159e-29	-14.41471	-25.65463	124.0966	1.129204e-27	0.0003787244			
rs7166206	3.021810e-28	-14.49570	-25.53945	121.8890	3.405146e-27	0.0004281220			
rs7183892	3.026646e-28	-14.06609	-25.22785	121.7699	3.614195e-27	0.0004281963			
rs6494411	3.297976e-28	-14.52451	-24.85527	121.8113	3.540073e-27	0.0004322039			
rs289818	3.376500e-28	-13.76605	-25.14802	121.4349	4.273124e-27	0.0004333089			
rs289816	3.644851e-28	-13.76605	-24.97999	121.3121	4.543623e-27	0.0004369199			
rs4411464	7.555834e-28	-13.29581	-25.19636	119.7212	1.006617e-26	0.0004729014			
rs4721415	1.472851e-27	15.05171	25.79182	118.9972	1.445717e-26	0.0005084603			
rs7178111	2.078104e-26	-11.81512	-24.75983	113.1243	2.725011e-25	0.0006781148			
rs7178104	2.941829e-26	-14.90122	-24.78222	113.4409	2.326075e-25	0.0007042824			

FALSE TRUE
479302 49977

Answer (Ex. 6) — The λ as reported by standard GenABEL procedure is huge:

```
lambda(qts0)$est
[1] 9.791453
```

Answer (Ex. 7) — No (see Pc1df in previous output)

Answer (Ex. 8) — The estimates of λ vary strongly depending on the method used:

```
# regression 100%
c2 <- qts0[, "chi2.1df"]
estlambda(c2)$est
# regression 95%
estlambda(c2, prop=0.95)$est
# mean
mean(c2)
# median
median(c2)/qchisq(.5, 1)
# trimmed mean at 95%
```

```

mean(sort(c2)[1:round(0.95*length(c2))])/((1/.95)*pchisq(qchisq(.95,df=1),df=3))
[1] 9.791453
[1] 11.04772
[1] 10.99943
[1] 13.64433
[1] 11.72667

```

Answer (Ex. 9) — One of the ways to answer this question is to look how close is the fit of the corrected test statistic to the null distribution. From the tests below it follows that the trimmed mean option is the best. Note, however, that you are working with the data *without any association*, and your results, strictly speaking, can not be generalized to a real situation when true associations are present.

```

sW <- getOption("warn")
options(warn=-1)
# regression 100%
c2 <- qts0[, "chi2.1df"]
lambda <- estlambda(c2)$est
c2c <- c2/lambda
ks.test(c2c, "pchisq", df=1)$stat
# regression 95%
lambda <- estlambda(c2, prop=0.95)$est
c2c <- c2/lambda
ks.test(c2c, "pchisq", df=1)$stat
# mean
lambda <- mean(c2)
c2c <- c2/lambda
ks.test(c2c, "pchisq", df=1)$stat
# median
lambda <- median(c2)/qchisq(.5, 1)
c2c <- c2/lambda
ks.test(c2c, "pchisq", df=1)$stat
# trimmed mean at 95%
lambda <- mean(sort(c2)[1:round(0.95*length(c2))])/((1/.95)*pchisq(qchisq(.95,df=1),df=3))
c2c <- c2/lambda
ks.test(c2c, "pchisq", df=1)$stat
options(warn=sW)
D
0.07522724

```

D
0.04939044
D
0.05027084
D
0.04587066
D
0.03788888

Answer (Ex. 10) — Lambda is very reasonable; there is GW-significant hit. Run the R code

```
qts <- qtscore(phe~sex,data=df,strata=phdata(df)$pop)
lambda(qts)$est
summary(qts)
[1] 1.006406
```

Summary for top 10 results, sorted by P1df

	Chromosome	Position	Strand	A1	A2	N	effB	se_effB	chi2.1df
rs10518394	1	72214606	+	C	T	210	6.579754	1.1440942	33.07468
rs10518395	1	72255233	+	T	C	210	6.409265	1.3215342	23.52121
rs7732608	5	1233959521	+	A	G	210	-2.743810	0.6037035	20.65668
rs4888646	16	3213669549	+	G	A	208	3.156958	0.7249879	18.96164
rs7513441	1	72196705	+	G	A	208	3.479265	0.8013470	18.85097
rs960529	12	2584310280	+	C	T	206	3.504380	0.8154756	18.46717
rs17721635	4	844039774	+	A	G	207	6.585803	1.5437516	18.19963
rs6751506	2	336097537	+	G	A	208	6.756108	1.6032181	17.75857
rs1860393	12	2494213167	+	G	A	208	3.064326	0.7385016	17.21738
rs3889228	16	3228175489	-	G	T	185	-2.574434	0.6205887	17.20901
	P1df	effAB	effBB	chi2.2df	P2df	Pc1df			
rs10518394	8.868594e-09	7.286720	12.331776	36.36228	1.270667e-08	9.882894e-09			
rs10518395	1.235445e-06	3.863802	21.732415	23.84868	6.627107e-06	1.335435e-06			
rs7732608	5.494514e-06	9.549322	11.524601	21.18435	2.511170e-05	5.885152e-06			
rs4888646	1.333728e-05	5.792755	14.970399	19.17415	6.860995e-05	1.420838e-05			
rs7513441	1.413392e-05	9.081618	11.912046	23.25607	8.912677e-06	1.505173e-05			
rs960529	1.728564e-05	3.318340	7.383783	20.68956	3.216015e-05	1.838556e-05			
rs17721635	1.989170e-05	24.301819	29.796347	18.32933	1.046732e-04	2.113937e-05			
rs6751506	2.507854e-05	11.706539	17.498339	17.89261	1.302172e-04	2.661401e-05			
rs1860393	3.333723e-05	7.522871	15.054994	18.67697	8.797244e-05	3.531720e-05			
rs3889228	3.348441e-05	-5.874787	-19.095723	17.30602	1.746003e-04	3.547218e-05			

Answer (Ex. 11) — Run the code

```
gIbs <- ibs(df)
diag(gIbs) <- 1
pcIbs <- cmdscale(as.dist(1-gIbs),k=10)
mlr10 <- mlreg(phe~sex+pcIbs[,1:10],data=df)
estlambda(mlr10[, "chi2.1df"])$est
summary(mlr10)
[1] 0.9936808
Summary for top 10 results, sorted by P1df
```

	Chromosome	Position	Strand	A1	A2	N	effB	se_effB	chi2.1df
rs10518394	1	72214606	+	C	T	210	6.690857	1.0809712	38.31204
rs10518395	1	72255233	+	T	C	210	6.860952	1.2829639	28.59828
rs960529	12	2584310280	+	C	T	206	3.984842	0.8018764	24.69491
rs6515824	20	3646777846	+	C	T	209	5.133286	1.1248409	20.82613
rs11077325	16	3144966713	+	G	A	210	5.767299	1.2699835	20.62285
rs3845906	3	655408823	-	T	C	204	-5.479251	1.2069263	20.61014
rs10050474	5	1103211963	+	A	G	209	7.882775	1.7407183	20.50696
rs4666808	2	479290594	+	T	C	210	6.730852	1.4882892	20.45340
rs4888646	16	3213669549	+	G	A	208	3.949398	0.8802285	20.13126
rs7732608	5	1233959521	+	A	G	210	-4.073474	0.9123340	19.93528

	P1df	Pc1df	effAB	effBB	chi2.2df	P2df
rs10518394	6.028952e-10	5.321370e-10	NA	NA	NA	NA
rs10518395	8.906122e-08	8.107796e-08	NA	NA	NA	NA
rs960529	6.716145e-07	6.190641e-07	NA	NA	NA	NA
rs6515824	5.029198e-06	4.693223e-06	NA	NA	NA	NA
rs11077325	5.592464e-06	5.222245e-06	NA	NA	NA	NA
rs3845906	5.629728e-06	5.257255e-06	NA	NA	NA	NA
rs10050474	5.941490e-06	5.550217e-06	NA	NA	NA	NA
rs4666808	6.110102e-06	5.708700e-06	NA	NA	NA	NA
rs4888646	7.230521e-06	6.762459e-06	NA	NA	NA	NA
rs7732608	8.010849e-06	7.496959e-06	NA	NA	NA	NA

Answer (Ex. 12) — `h2 <- polygenic(phe~sex,data=df,kin=(gIbs/2),quiet=TRUE)`

```
h2$est
mmsIbs <- mmscore(h2,data=df)
lambda(mmsIbs)
summary(mmsIbs)
[1] 0.9999991
$estimate
```



```
[1] 1.116662
```

```
$se
```

```
[1] 3.659768e-05
```

```
Summary for top 10 results, sorted by P1df
```

	Chromosome	Position	Strand	A1	A2	N	effB	se_effB	chi2.1df
rs17675813	16	3206116502	+	G	A	188	-6.705347	1.2303213	29.70335
rs4772447	13	2774249004	+	G	A	180	-5.772128	1.0643268	29.41182
rs12441236	15	3053517961	+	G	A	185	-6.175968	1.1398250	29.35849
rs10976178	9	1939841622	+	C	T	185	-5.298327	0.9795148	29.25874
rs1863188	2	514484026	-	C	T	175	-5.490856	1.0260496	28.63804
rs9988693	10	2126599674	+	G	T	181	6.156263	1.1504974	28.63275
rs10518394	1	72214606	+	C	T	210	6.847941	1.2800644	28.61912
rs17615522	4	875799875	+	A	C	195	-5.695996	1.0816857	27.72919
rs749873	2	433156296	+	C	T	195	7.221541	1.4278989	25.57790
rs10988617	9	2064525746	+	C	T	192	-5.310638	1.0511805	25.52341

	P1df	Pc1df	effAB	effBB	chi2.2df	P2df
rs17675813	5.034782e-08	2.502263e-07	NA	NA	0	NA
rs4772447	5.851958e-08	2.864359e-07	NA	NA	0	NA
rs12441236	6.015244e-08	2.936076e-07	NA	NA	0	NA
rs10976178	6.332997e-08	3.075077e-07	NA	NA	0	NA
rs1863188	8.725107e-08	4.101178e-07	NA	NA	0	NA
rs9988693	8.749009e-08	4.111273e-07	NA	NA	0	NA
rs10518394	8.810769e-08	4.137344e-07	NA	NA	0	NA
rs17615522	1.395409e-07	6.254298e-07	NA	NA	0	NA
rs749873	4.248779e-07	1.701477e-06	NA	NA	0	NA
rs10988617	4.370478e-07	1.745226e-06	NA	NA	0	NA

Answer (Ex. 13) — The best analysis method is stratified analysis and/or the PCA-based analysis. These do reflect the design of the study and produces reasonable GC λ .

5 Appendix B: Generation of the data set

```
library(GenABEL)
load("data/HapMap_r21_550K.RData")
chr <- chromosome(hapmap550k)
qc <- check.marker(hapmap550k[, (chr=="21" | chr=="X" | chr=="Y")])
phdata(hapmap550k)$sex[which(idnames(hapmap550k) %in% qc$ismale)] <- 1
hapmap550k@gtdata@male <- phdata(hapmap550k)$sex
```

```

df <- hapmap550k[,autosomal(hapmap550k)]
gIbs <- ibs(df,weight="no")
gIbd <- ibs(df,weight="freq")
attach(phdata(df))

nPolySnps <- 10000
popMu=list(CHB=160,JPT=165,YRI=170,CEU=180)
popVar=list(CHB=49,JPT=25,YRI=64,CEU=25)
betaSex <- 12
varG <- 2*25
set.seed(9)
polySnps <- sample(snpnames(df),nPolySnps)
polyX <- scale(as.numeric(gtdata(df[,polySnps])))
any(is.na(polyX))
polyX[is.na(polyX)] <- 0
any(is.na(polyX))
G <- as.vector( polyX %*% rep(0.1,nPolySnps) )
var(G)
G <- G + as.vector( polyX[,1:2] %*% c(25,30) )
colnames(polyX)[1:2]
var(G)
G <- G/sd(G)
G <- G*sqrt(varG)
phe <- sex*betaSex + G - 10
for (cPop in names(popMu)) {
  cIds <- which(pop == cPop)
  phe[cIds] <- phe[cIds] + popMu[[cPop]] + rnorm(length(cIds),sd=sqrt(popVar[[cPop]]))
}
phdata(df)$phe <- phe
summary(lm(phe~sex,data=phdata(df)))
summary(lm(phe~sex+pop,data=phdata(df)))
save(df,file="data/hm.RData")

```

Loading required package: MASS
 GenABEL v. 1.7-4 (February 03, 2013) loaded

Installed GenABEL version (1.7-4) is not the same as stable version available from CRAN (1.7-3). Unless used intentionally, consider updating to the latest CRAN version. For that, use 'install.packages("GenABEL")', or ask your system administrator

to update the package.

Excluding people/markers with extremely low call rate...

21182 markers and 210 people in total

0 people excluded because of call rate < 0.1

0 markers excluded because of call rate < 0.1

Passed: 21182 markers and 210 people

Running sex chromosome checks...

0 heterozygous X-linked male genotypes found

0 X-linked markers are likely to be autosomal (odds > 1000)

0 male are likely to be female (odds > 1000)

105 female are likely to be male (odds > 1000)

0 people have intermediate X-chromosome inbreeding ($0.5 > F > 0.5$)

If these people/markers are removed, 0 heterozygous male genotypes are left

Warning in check.marker(hapmap550k[, (chr == "21" | chr == "X" | chr == :

The number of Y-chromosome SNPs is low (6). Consider ignoring Y-checks by setting 'X

0 possibly female Y genotypes identified

None of these people excluded based on Y-threshold of 0.8

Passed: 21182 markers and 105 people

Checking Y-chromosome heterozygous genotypes... 0 (NaN %) found.

no X/Y/mtDNA-errors to fix

RUN 1

21182 markers and 105 people in total

303 (1.43046%) markers excluded as having low (<2.380952%) minor allele frequency

635 (2.997828%) markers excluded because of low (<95%) call rate

5962 (28.14654%) markers excluded because they are out of HWE (FDR <0.2)

2 (1.904762%) people excluded because of low (<95%) call rate

Mean autosomal HET is 0.3194573 (s.e. 0.01776116)

0 people excluded because too high autosomal heterozygosity (FDR <1%)

Mean IBS is 0.7203834 (s.e. 0.02325525), as based on 2000 autosomal markers

0 (0%) people excluded because of too high IBS (>=0.95)

In total, 14481 (68.36465%) markers passed all criteria

In total, 103 (98.09524%) people passed all criteria

RUN 2

14481 markers and 103 people in total
 26 (0.1795456%) markers excluded as having low (<2.427184%) minor allele frequency
 0 (0%) markers excluded because of low (<95%) call rate
 0 (0%) markers excluded because they are out of HWE (FDR <0.2)
 0 (0%) people excluded because of low (<95%) call rate
 Mean autosomal HET is 0.3203484 (s.e. 0.01720416)
 0 people excluded because too high autosomal heterozygosity (FDR <1%)
 Mean IBS is 0.7197077 (s.e. 0.02371458), as based on 2000 autosomal markers
 0 (0%) people excluded because of too high IBS (>=0.95)
 In total, 14455 (99.82045%) markers passed all criteria
 In total, 103 (100%) people passed all criteria

RUN 3

14455 markers and 103 people in total
 0 (0%) markers excluded as having low (<2.427184%) minor allele frequency
 0 (0%) markers excluded because of low (<95%) call rate
 0 (0%) markers excluded because they are out of HWE (FDR <0.2)
 0 (0%) people excluded because of low (<95%) call rate
 Mean autosomal HET is 0.3203484 (s.e. 0.01720416)
 0 people excluded because too high autosomal heterozygosity (FDR <1%)
 Mean IBS is 0.7234528 (s.e. 0.02411495), as based on 2000 autosomal markers
 0 (0%) people excluded because of too high IBS (>=0.95)
 In total, 14455 (100%) markers passed all criteria
 In total, 103 (100%) people passed all criteria
 [1] TRUE
 [1] FALSE
 [1] 2985.701
 [1] "rs1377826" "rs10518394"
 [1] 4994.655

Call:

lm(formula = phe ~ sex, data = phdata(df))

Residuals:

	Min	1Q	Median	3Q	Max
	-37.547	-11.887	0.114	11.912	31.952

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	160.313	1.460	109.798	< 2e-16 ***

```

sex          11.569      2.065    5.603 6.63e-08 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 14.96 on 208 degrees of freedom
Multiple R-squared:  0.1311,    Adjusted R-squared:  0.127
F-statistic: 31.39 on 1 and 208 DF,  p-value: 6.633e-08

Call:
lm(formula = phe ~ sex + pop, data = phdata(df))

Residuals:
    Min       1Q   Median       3Q      Max
-21.3562  -4.7761  -0.0142   5.3910  21.3648

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)   176.352     1.170  150.686  <2e-16 ***
sex           11.517     1.103   10.437  <2e-16 ***
popCHB        -32.230     1.577  -20.443  <2e-16 ***
popJPT        -26.742     1.577  -16.961  <2e-16 ***
popYRI        -11.816     1.460   -8.095   5e-14 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.995 on 205 degrees of freedom
Multiple R-squared:  0.7555,    Adjusted R-squared:  0.7507
F-statistic: 158.3 on 4 and 205 DF,  p-value: < 2.2e-16

```